Homogeneous studies of transiting extrasolar planets – I. Light-curve analyses

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ABSTRACT
I present a homogeneous analysis of the transit light curves of 14 well-observed transiting extrasolar planets. The light curves are modelled using JKTEBOP, random errors are measured using Monte Carlo simulations and the effects of correlated noise are included using a residual-permutation algorithm. The importance of stellar limb darkening on the light-curve solutions and parameter uncertainties is investigated using five different limb darkening laws and including different numbers of coefficients as fitted parameters. The linear limb darkening law cannot adequately fit the Hubble Space Telescope (HST) photometry of HD 209458, but the other four laws give very similar results to each other for all transit light curves. In most cases fixing the limb darkening coefficients at theoretically predicted values does not bias the results, but does cause the error estimates to be too small. The available theoretical limb darkening coefficients clearly disagree with empirical values measured from the HST light curves of HD 209458; limb darkening must be included as fitted parameters when analysing high-quality light curves.

In most cases the results of my analysis agree with the values found by other authors, but the uncertainties I find can be significantly larger (by factors of up to 3). Despite these greater uncertainty estimates, the analyses of sets of independent light curves for both HD 189733 and HD 209458 lead to results which do not agree with each other. This discrepancy is worst for the ratio of the radii (6.7σ for HD 189733 and 3.7σ for HD 209458), which depends primarily on the depth of the transit. It is therefore not due to the analysis method but is present in the light curves. These underlying systematic errors cannot be detected from the reduced data alone unless at least three independent light curves are available for an individual planetary system.

The surface gravities of transiting extrasolar planets are known to be correlated with their orbital periods. New surface gravity values, calculated from the light-curve results and the stellar spectroscopic orbits, show that this correlation is still present. New high-precision light curves are needed for HD 149026, OGLE-TR-10, OGLE-TR-56, OGLE-TR-132 and GJ 436, and new radial velocity curves for the XO-1, WASP-1, WASP-2 and the OGLE (Optical Gravitational Lensing Experiment) planetary systems.

Key words: binaries: eclipsing – stars: fundamental parameters – planetary systems.

1 INTRODUCTION
The discovery of extrasolar planets was one of the great scientific achievements of the twentieth century (Mayor & Queloz 1995), made possible by technological advances in stellar spectroscopy (e.g. Butler et al. 1996). At this point over 200 exoplanets have been discovered through radial velocity monitoring of their parent stars, making this technique very successful (Udry & Santos 2007). The limitation of the method is that it is not possible to directly measure any planetary properties: for each system only lower limits on the mass and orbital separation of the planet can be obtained.

The solution to this problem arrived 5 yr later, with the first detection of the transit of an extrasolar planet across the disc of its parent star, HD 209458 (Charbonneau et al. 2000; Henry et al. 2000). Since then over 30 transiting extrasolar planetary systems (TEPs) have been discovered, the majority by wide-field photometric variability surveys. Much more information is available for TEPs because the light-curve shape is sensitive to the sizes of the star and planet and the inclination of the orbit.

From the study of the light curve of a TEP, the spectroscopic orbit of the star, and one additional piece of information (often a constraint on the stellar mass using theoretical models), it is possible...
to precisely measure the masses, radii, surface gravities and densities of both the star and the planet. This powerful procedure then allows detailed investigations into the chemical composition of the planet and the physical processes which govern its properties and evolution.

The characteristics of the known TEPs have been derived in this way by many authors, but using several analysis techniques and a wide variety of observational and theoretical constraints. Considering only the light-curve analyses, various studies have used different limb darkening (LD) functions and in many cases the coefficients of these functions have been fixed at theoretically predicted values without any consideration of whether this approach might introduce systematic errors into the results. It is important to pay attention to the effects of LD when modelling the light curves of TEPs because the coefficients may be correlated with the other parameters and so affect the measurement of the physical properties of the system as a whole. In light of this, it is appropriate to concentrate on studying the known TEPs to obtain their properties as accurately and as homogeneously as possible.

In this work I present light-curve analyses for all 14 TEPs for which decent light curves are available. Each system is studied using the same methods to ensure that the results are as homogeneous and reliable as possible. A requirement of this method is that the importance of effects such as LD must be quantified so the best approach can be identified and used for every system.

To enable a homogeneous study of the light curves of TEPs I investigate the following questions: Is linear LD an acceptable approximation? Is it possible to measure accurate LD coefficients (LDCs) from the data? Are these coefficients consistent with theoretical predictions? How accurately can orbital inclinations be measured from individual light curves? How important are correlated errors in each light curve?

The results of this analysis make it possible to answer further questions: Do the results in this work agree with published values? Do independent light curves of the same TEP agree with each other? If not, what is the size of the systematic error which causes the disagreement? How well understood are the properties of the known TEPs?

In addition to dealing with these questions, I identify which of the studied TEPs would benefit the most from further study, both photometric and spectroscopic. Finally, I measure the surface gravities of each planet directly from the light-curve parameters and the velocity amplitude of the parent star, using the method introduced by Southworth et al. (2004c) and Southworth, Wheatley & Sams (2007b). In a second paper (in preparation) the results presented here are used to determine the physical properties of the planets and stars in these systems using additional constraints from theoretical models, paying close attention to random and systematic errors and to the inter-agreement of independent sets of stellar evolutionary models.

2 MODELLING THE LIGHT CURVES OF TRANSITING EXTRASOLAR PLANETARY SYSTEMS

A TEP is simply a special case of an eclipsing binary system. The study of eclipsing binary light curves has been part of stellar astrophysics for many years, and was originally put on a solid foundation by Russell (1912a,b). Russell’s technique, sometimes referred to as ‘rectification’, was successively refined (see Russell & Merrill 1952; Kopal 1959) but still requires several approximations which are not appropriate for many systems.

When computers became widely available the Russell–Merrill method was superseded by models based on numerical integration, including the Wilson–Devinney code (Wilson & Devinney 1971; Wilson 1979, 1993) WINK (Wood 1971, 1973), EBOP (Etzel 1975; Popper & Etzel 1981) and others (Hill 1979; Hadrava 1990), whose use is widespread. More recently, Mandel & Agol (2002) and Giménez (2006) have produced fully analytical models which are intended for the study of TEPs. This approach allows a very fast computation, but requires approximations such as the assumption of spherical shapes.

One feature of a TEP system is that the radii of the two components are very different, which can be taxing for models based on numerical integration over the surfaces of the components. Those models which use Roche geometry (e.g. the Wilson–Devinney code) simulate the component surfaces using several thousands of points each. This means that they very accurately reproduce distorted surfaces, but can be crippled by numerical error when the planet is so small that it only covers a small fraction of the points on the stellar surface. However, the use of a fully analytic model, with its accompanying requirement of sphericity, can potentially lead to an unquantifiable systematic error in TEPs where the planet is distorted because it is very close to the star.

In this work I adopt the EBOP model (Etzel 1975, 1981; Popper & Etzel 1981), which simulates the components of an eclipsing binary system using biaxial ellipsoids. It can also be restricted to spherical objects, so systematic effects arising from the assumption of a physical shape can be easily quantified. EBOP uses numerical integration in concentric annuli over the surface of each component (Nelson & Davis 1972), an approach which requires only a modest amount of computation and has a much lower numerical error than other non-analytic codes (Etzel 1975).

I use the JKTEBOP code,1 a heavily modified version of EBOP (Southworth, Maxted & Smalley 2004a,b) which incorporates the Levenberg–Marquardt optimization algorithm (MRQMIN; Press et al. 1992, p. 678), an improved treatment of LD, and extensive error analysis techniques. The EBOP model has been shown to work well for TEPs by a number of authors, including Giménez (2006), Wilson et al. (2006), Shporer et al. (2007) and Southworth et al. (2007b).

2.1 What does a transit light curve tell us?

An accurate orbital period, \(P_{\text{orb}}\), and reference time of minimum light, \(T_0\), are available for all systems studied in this work. Apart from \(P_{\text{orb}}\) and \(T_0\), the light curve of a TEP depends mainly on three quantities, which can be expressed in several different ways. In this work I take the quantities to be the fractional radii of the two stars and the orbital inclination, \(i\). The fractional radii are defined as:

\[
r_A = \frac{R_A}{a}, \quad r_p = \frac{R_p}{a},
\]

where \(R_A\) and \(R_p\) are the (absolute) stellar and planetary radii and \(a\) is the orbital semimajor axis. There are three main directly measurable quantities: the transit depth, its overall duration and duration of

1 JKTEBOP is available from http://www.astro.keele.ac.uk/~jkt/codes.html

2 Throughout this work I identify stellar parameters with a subscripted ‘A’ and planet parameters with a subscripted ‘b’ to conform to IAU nomenclature. I have neglected the usual subscripts ‘s’ and ‘p’ as these can lead to confusion (‘s’ for TEPs refers to the star but for eclipsing binaries has been used to designate the secondary component; ‘p’ likewise could mean ‘planet’ or conversely ‘primary’ in the different communities).
the fractional radii \( r_A, r_B \) and \( i \) can be measured accurately from these three main quantities.

It is common in the literature to state that ordinary light curves do not reach the accuracy required to lift the degeneracy between \( i \) and \( R_A \) (e.g. Rowe et al. 2007). A transit light curve has three main observable properties and depends on three main physical properties, so such a statement is incorrect. The crucial advantage the study of TEPs has over that of eclipsing binaries is that the optical light produced by the planet can be assumed to be zero, thus reducing the number of light-curve parameters from four to three. The results obtained in this and other works demonstrate that ground-based light curves can provide definitive results for TEPs.

Note that (apart from \( P_{	ext{orb}} \)) a light curve holds no information about the overall scale of the system so is not directly dependent on the mass or absolute radius of either component.

2.2 Solution procedure

Rather than fitting for \( R_A \) and \( r_B \) directly, JKTEBOP fits for the sum of the fractional radii \( (r_A + r_B) \) and the ratio of the radii \( k \) (Southworth et al. 2005). This is because these quantities are only very weakly correlated for a wide variety of light-curve shapes, which improves solution convergence. In the analyses presented in this work I have always fitted for \((r_A + r_B), k, i \) and \( T_0 \).

The period, \( P_{	ext{orb}} \), is generally known with much more accuracy than any other parameter, so I have usually fixed it at a known value. In most cases the orbital eccentricity, \( e \), is set to zero (see Laughlin et al. 2005 for a well-presented study of previous claims of a non-zero eccentricity for HD 209458) and the planet is assumed to produce no light (an excellent approximation at optical wavelengths).

The mass ratio, which in EBOP governs how aspherical the planet is, is fixed at an appropriate value. The mass ratio has a negligible effect on the solutions (changes by a factor of 2 are unimportant). I emphasize that the mass ratio values adopted here are not otherwise used in the determination of the properties of the TEPs. To obtain a high numerical accuracy I set the size of the integration annuli (parameter ‘INTRING’ in EBOP) to be 1". LD is also included using one of five different laws (see Section 2.3).

One potential problem in analysing TEP light curves is that any additional light contribution from a nearby star will decrease the transit depth and cause a systematic error in the measured fractional radii of the two components. There is unfortunately no way of detecting ‘third light’ from a transit light curve alone: including it as a fitted parameter will render the solution thoroughly indeterminate. Thankfully, the possibility of a blend is one of the basic tests performed by transit search projects to ensure a candidate TEP is not a false positive (e.g. Weldrake et al. 2008). The spectra of all confirmed TEPs have also received intense scrutiny and none has been found to contain light contamination from a third body. Third light can therefore be ruled out at roughly the 5 per cent level for most systems. This amount of third light is in most cases insufficient to cause an important systematic error in the measured fractional radii.

One of the assumptions of the light-curve models used here and elsewhere is that the component bodies can be represented by geometrical shapes with definite edges. This assumption does not necessarily correspond to the canonical theoretical approach of defining a stellar or planetary surface as the point at which the optical depth is \( \tau = 2/3 \). This effect has been considered in detail by Burrows et al. (2007), who find that for a highly irradiated low-gravity planet the difference in radius can be up to 5 per cent. This effect must be borne in mind during any comparisons between observed and theoretically predicted planetary radii.

2.3 Treatment of the stellar limb darkening

LD is an important effect in light-curve analysis of TEPs as it has a small but significant effect on the entire light-curve shape. This is often included using the simple linear law (Russell 1912b):

\[
I_\mu = I_0 [1 - u(1 - \mu)],
\]

where \( \mu = \cos \gamma \) and \( \gamma \) is the angle between the surface normal and the line of sight. \( I_0 \) is the intensity at the centre of the stellar disc, \( I_\mu \) is the intensity at angle \( \gamma \) and \( \mu \) is the LDC. The linear LD law is known to be a poor approximation to the predictions of model atmospheres (e.g. Van Hamme 1993). There is also evidence that it performs less well than more complex laws, at least at optical blue and visual wavelengths, in eclipsing binaries (Southworth, Bruntt & Buzasi 2007a) and in TEPs (Southworth et al. 2007b).

A currently unanswered question in the study of TEPs is how important is LD, and does the use of different laws make much difference to the light-curve results? I have therefore implemented a number of other LD laws into JKTEBOP and used them in the light-curve modelling process. These include the quadratic law (Kopal 1950):

\[
I_\mu = I_0 [1 - u_q(1 - \mu) - v_q(1 - \mu^2)],
\]

where the linear LDC is \( u_q \) and the non-linear LDC is \( v_q \); the square-root law (Díaz-Cordovés & Giménez 1992):

\[
I_\mu = I_0 [1 - u(1 - \mu) - v(1 - \sqrt{\mu})],
\]

and the logarithmic law (Klinglesmith & Sobieski 1970):

\[
I_\mu = I_0 [1 - u(1 - \mu) - v \mu \ln \mu].
\]

I have also used the cubic law (van’t Veer 1960; see also Barban et al. 2003):

\[
I_\mu = I_0 [1 - u_c(1 - \mu) - v(1 - \mu^3)],
\]

but this is complicated by the unavailability of theoretically predicted LDCs.

In Southworth et al. (2007a) it was found that the square root and quadratic LD laws gave significantly better results than the linear law for an eclipsing binary with partial eclipses. Attempts to derive both linear and non-linear LDCs for each star were successful, but gave imprecise results because the two LDCs for one object are strongly correlated (Southworth et al. 2007a, their fig. 3). A similar situation was consistently found in the current work (see Fig. 2). We can draw three conclusions from this: (1) non-linear LD laws should be used; (2) in most cases it is sufficient to fix one LDC at a reasonable value and fit for only the second LDC; (3) using LD laws with three or more LDCs (e.g. the four-coefficient law introduced by Claret 2000) is unnecessary for data of the level of accuracy currently achievable.

When modelling the light curves in this work I have calculated solutions for all five LD laws given above. I have always tried to fit for two LDCs when using a non-linear law. In those cases where this did not give reasonable results, I have fixed the non-linear LDC to a reasonable (theoretically predicted) value and fitted for the linear LDC. In a few cases this has also delivered unphysical results, so both LDCs had to be fixed to theoretical values. When an LDC was fixed, its value was perturbed in the error analysis to ensure that this source of error was included in the results. In every case the applied perturbations followed a flat distribution of \( \pm 0.1 \) around the fixed value. Although some non-linear LDCs were fixed to theoretically predicted values, in these cases the linear and non-linear LDCs were so strongly correlated that this introduces only an infinitesimal
dependence on theoretical model atmospheres. For a few systems I have also presented, for illustration and comparison with other studies, solutions with both LDCs fixed and also not perturbed.

Other researchers have fitted linear combinations of LDCs, for example $2u_q + v_q$ and $u_q - 2v_q$ for the quadratic law (e.g. Winn, Holman & Rousanuova 2007d). These combinations are less strongly correlated than $u_q$ and $v_q$ so their values can be found more precisely. Using these combinations can improve convergence when fitting observational data, but I find that they do not lead to more precise measurements for $u_q$ and $v_q$. I have not used these combinations for two reasons: no problems with convergence have been noticed; and $u$ and $v$ are more straightforwardly comparable to model predictions.

Theoretically predicted LDCs were obtained by bilinear interpolation in the stellar $T_{\text{eff}}$ and surface gravity, $^{3}$ using the tabulations provided by Van Hamme (1993), Claret et al. (1995), Díaz-Cordovés, Claret & Giménez (1995), Claret (2000, 2004) and Claret & Hauschildt (2003).

2.4 Error analysis

The formal parameter uncertainties produced by MRQMIN are calculated from the solution covariance matrix and are unreliable in the presence of parameter correlations (Popper 1984; Maceroni & Rucinski 1997; Southworth & Clausen 2007), so have been ignored in this work. To calculate the random errors on the light-curve parameters I have used the Monte Carlo simulation algorithm implemented in JKTEBOP (Southworth et al. 2004b,c), which was found to give reliable results by Southworth et al. (2005).

The Monte Carlo algorithm finds the best fit to the actual data and uses this to generate a model light curve with the same time sampling. Then Gaussian noise is added and the resulting synthetic light curve is fitted in the same way as the actual data. The latter step is performed many times, and the 1σ uncertainties in the measured light-curve parameters are assessed from the distribution of the best fits to the simulated light curves. A vital part of this process is that substantial random perturbations are applied to the initial parameter values before fitting each simulated light curve. This allows a detailed exploration of the parameter space and of parameter correlations, and so gives similar results to the Markov Chain Monte Carlo techniques used by other researchers (e.g. Holman et al. 2006).

For each analysis I have used 1000 Monte Carlo simulations, which is a good compromise between avoiding small-number statistics and requiring a large amount of CPU time.

Whilst the random errors are straightforward to quantify, the presence of correlated ‘red’ noise can cause systematic errors which the Monte Carlo algorithm will not properly account for. This is a widespread problem in the study of TEPs because changes in airmass, telescope pointing and focus, detector response and other effects can cause significant correlations between adjacent data points in a light curve. Problems can also be caused by the data reduction technique. Unfortunately, there is no general way of completely removing these effects from a light curve. An excellent example of systematic bias is given by Gillon et al. (2007a), who demonstrate that the depth of an observed transit of OGLE-TR-132 varies depending on exactly how the data reduction is performed. This bias could not be detected from the reduced light curve alone. A detailed investigation of how red noise affects the analysis of TEPs is given by Pont, Zucker & Queloz (2006).

To assess the effect of systematic errors on the uncertainties of the light-curve parameter measurements, I have implemented into JKTEBOP a residual-permutation (or ‘prayer bead’) algorithm (Jenkins, Caldwell & Borucki 2002). In this method, the residuals around the best-fitting light-curve solution are all shifted to the next data point. A new fit is found, then the residuals are shifted again, with those which drop off the end of the data set being wrapped around to the start of the data. This process continues until the residuals have cycled back to where they originated, and results in a distribution of fitted values for each parameter from which its uncertainty can be estimated. The residual-permutation algorithm gives reliable and easily interpretable results, but its statistical properties are not totally clear and it is only sensitive to correlated noise on time-scales different to the eclipse duration. The method has been used before on several TEPs (e.g. Bouchy et al. 2005a; Pont et al. 2005; Gillon et al. 2007b; Knutson et al. 2007d).

For each light curve I have used the residual permutation algorithm to assess the importance of systematic errors. In those cases where it gives larger parameter uncertainties than the Monte Carlo algorithm, which only considers Poisson noise, I have adopted the residual permutation results, which are sensitive to both Poisson and correlated noise. The parameter error estimates presented in this work also include a contribution from the effects of using different LD laws, and in every case are 1σ errors. When observational errors are available I have used these to set the size of the Gaussian noise level for the Monte Carlo analysis. In cases where this resulted in a reduced $\chi^2(\nu_{\text{red}})$ of greater than unity I have multiplied the Monte Carlo errors by $\sqrt{\nu_{\text{red}}}$ to compensate for the underestimated observational errors (Bruntt et al. 2006; Southworth et al. 2007a).

3 RESULTS FOR EACH SYSTEM

Below I present an analysis of the available light curves of each TEP for which good or definitive data are available. For each light curve a set of solutions is tabulated for each of the five LD laws and for fitting either one or two LDCs. As these tables are quite bulky they have been shifted to Appendix A. Please see the Supplementary Material section for details. For each system there is also a table comparing the final light-curve parameters with those from previous analyses.

The TEPs are discussed in rough order of increasing complexity, starting with the TrES, XO and WASP and HAT systems. The TEPs discovered using photometry from the OGLE project follow; these are in general a bit more difficult to analyse because they are fainter and so have less good light curves. GJ 436 is then discussed on the basis of infrared observations from the Spitzer Space Telescope; this analysis is more complicated as the orbit is eccentric and the light produced by the planet is not negligible. Finally, I investigate HD 149026, HD 189733 and HD 209458. Whilst the very shallow transit of HD 149026 makes it difficult to study, the brightness of the last two objects means that the available observations of them are of remarkable quality.

3.1 TrES-1

TrES-1 was discovered to be a TEP by the Trans-Atlantic Exoplanet Survey. Alonso et al. (2004) presented discovery light curves,

\footnote{The code for obtaining theoretically predicted LDCs by bilinear interpolation is called JktlD and is available from http://www.astro.keele.ac.uk/~jkt/codes.html}

\footnote{http://www.astrouw.edu.pl/~ogle/}
follow-up photometry and high-precision radial velocities which showed it to have a radius similar to that of Jupiter but a significantly lower mass. An excellent $\gamma$-band light curve of TrES-1 was obtained by Winn et al. (2007d) and covers three consecutive transits. The analysis of these data by Winn et al. (2007d) used quadratic LD, with the LDCs encouraged towards theoretically predicted values by the inclusion of a mild penalty term in the figure of merit. TrES-1 has also been studied by Steffen & Agol (2005), who found no evidence of a third planet from analysis of published times of transit, and by Knutson et al. (2007a), who were not able to detect a secondary eclipse from a ground-based $L$-band light curve.

I have modelled the Winn et al. (2007d) light curve of TrES-1 (1149 data points), adopting $P_{\text{orb}} = 3.030065$ d and fitting for the mid-point of the second of the three transits. A circular orbit was adopted, along with a mass ratio of $q = 0.00085$ (Winn et al. 2007d). Solutions have been calculated for three scenarios: (1) LDCs fixed at theoretical values; (2) including the linear LDC as a fitted parameter, and fixing the non-linear LDC at a theoretical value (and perturbing it during the Monte Carlo analysis to ensure this approach is reflected in the uncertainties); and (3) fitting for both linear and non-linear LDCs. The solutions are given in Table A1.

TrES-1 is unusual among the systems studied in this work in that the non-linearity of its LD is very small. The lowest residuals are, as expected, found for solutions where both LDCs are allowed to vary. Solutions with the linear LD as a fitting parameter but the non-linear LDC fixed are in good agreement with solutions with both LDCs fitted. However, the solutions where the LDCs are held fixed at theoretical values differ in two ways: the parameters are slightly different (and in the case of $r_b$ the discrepancy is significant) and the error bars are lower.

The solutions in which at least one LDC is a fitted parameter are in good agreement with each other. As the values are well defined even when both LDCs are fitted, I have used these in calculating the final solutions. The solutions with both LDCs fixed at theoretical values have been rejected, because we unfortunately cannot trust theoretical LDCs (see Section 3.14). For the linear law, the best-fitting $h_A$ does not agree with theoretical predictions. The best light-curve fit for the adopted solution type and the quadratic LD law is shown in Fig. 1 along with the observations and the residuals.

The residual perturbation results are in good agreement with the Monte Carlo results, which indicates that systematic errors are not important for these data. The final results from this study are given in Table 1 and compared to published studies. The results presented by Winn et al. (2007d) are in good agreement, but are closer to the solutions I find when fixing both LDCs. This is expected, because Winn et al. (2007d) included a penalty term in their figure of merit to encourage the LDCs to be close to theoretical values. Both the Winn et al. (2007d) and Alonso et al. (2004) quote smaller error bars than found in the present study. This is not surprising given the inclusion of additional error sources in the current work (e.g. the effect of different LD laws and the inclusion of the LDCs as fitted parameters), and confirms that the Monte Carlo analysis algorithm in JKTEBOP is reliable in the presence of parameter correlations.

### 3.1.1 Parameter correlations

Fig. 2 shows example plots of the output of the JKTEBOP Monte Carlo analysis algorithm for TrES-1. The first four panels show the joint distributions of parameter values for $r_A$, $r_b$, $k$, $(r_A + r_b)$ and $i$. There is a clear correlation between $r_A$ and $r_b$ and a strong correlation between $r_A$ and $k$. The latter correlation is expected because $k$ is very well determined (as it primarily depends on the eclipse depth). The parameters $(r_A + r_b)$ and $k$ are only weakly correlated, vindicating their use as parameters of the fit.

The lower half of Fig. 2 presents the Monte Carlo output for the LDCs for the four different non-linear LD laws. Strong correlations are seen for all four laws, which is expected because the light curves do not contain enough information on LD to obtain well-determined values for two LDCs; this situation is very similar to that for the partially eclipsing binary system $\beta$ Aurigae (Southworth et al. 2007a). The strongest correlation is seen for the square-root LD law and the weakest correlation for the cubic law, but these correlations have no clear effect on the other light-curve parameters (Table A1). This means that the cubic LDCs are the best determined, so the cubic LD law should be used if the LDCs are considered to be interesting in their own right.

Fig. 3 shows the very weak dependence of the derived $r_A$ and $r_b$ on the LDCs for the square-root law. Very little correlation can be seen, which confirms that the values of the LDCs have very little effect on those for the fractional radii of the components. The square-root law was used for this comparison because it is expected to have the strongest correlations (see Fig. 2).

### 3.2 TrES-2

TrES-2 was the second TEPs discovered by the Trans-Atlantic Exoplanet Survey (O’Donovan et al. 2006) and is both larger and more massive than Jupiter. Excellent $\gamma$-band light curves of three transits were presented and analysed by the TLC project (Holman et al. 2007b), who worked in close collaboration with Sozzetti et al. (2007) to obtain a highly accurate and consistent set of properties for the system. Its relatively low orbital inclination (i.e. high impact parameter) means that the fractional radii of the two components can be determined to a high accuracy.

I have studied the light curve obtained by Holman et al. (2007b), which contains 1033 data points and is superior to those presented in the discovery paper (O’Donovan et al. 2006). I assumed a mass ratio...
Table 1. Final parameters of the fit to the Winn et al. (2007d) light curve of TrES-1 from the JKTEBOP analysis. These have been compared to the properties of TrES-1 found by Winn et al. (2007d) and Alonso et al. (2004). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

| \( \sum (r_A + r_b) \) & 0.1097 ± 0.0022 & 0.1088  \\
| Ratio of the radii & 0.1381 ± 0.0014 & 0.1368 ± 0.00082 & 0.130 ± 0.006  \\
| Orbital inclination (°) & 88.67 ± 0.71 & >88.4 & 88.5 ± 1.23  \\
| Fractional stellar radius & 0.0964 ± 0.0018 & 0.0957 ± 0.0014  \\
| Fractional planetary radius & 0.01331 ± 0.00035 & 0.01308 ± 0.00023 & 0.01279  \\

Figure 2. Scatter plots showing some results of the Monte Carlo analysis used to measure the uncertainties in the light-curve parameters. The upper four panels show results obtained using linear LD: it can be seen that \( r_A \) and \( (r_A + r_b) \) are strongly correlated with each other in this representative case, whilst \( r_b \) and \( i \) are also correlated. The lower four panels show the correlations between the two LDCs for each of the non-linear LD laws: the correlation is the strongest for square root and weakest for cubic.

Figure 3. Scatter plots similar to Fig. 2 but showing the weakness of the correlations between the LDCs and the fractional radii of the star and planet. The square-root LD law was used for the results in this plot as this law should show the strongest correlations.

Figure 4. Phased light curve of the transits of TrES-2 from Holman et al. (2007b) compared to the best fit found using JKTEBOP and the quadratic LD law with the linear LDC included as a fitted parameter. The residuals of the fit are plotted at the bottom of the figure, offset from zero.
of 0.0012 (Holman et al. 2007b; Sozzetti et al. 2007) and fitted for the orbital period as the Holman et al. data cover 13 orbital cycles.

The results of the JKTEBOP analysis are given in Table A2 and the best fit for the quadratic LD law is shown in Fig. 4. The solutions where both LDCs are fitted return scattered results and very uncertain values for the coefficients, so these have been rejected. The solutions with one fitted LDC are well defined and in good agreement with each other (using the different LD laws), so have been adopted when calculating the final results. Solutions with both LDCs fixed give parameter values in good agreement with the adopted results, but the error bars are substantially smaller (as also found for TrES-1). It seems that solutions with LDCs fixed at theoretical values not only can give biased results, but also give error estimates which are artificially small. These solutions should only be used when there is no alternative.

For the uncertainties in the light-curve parameters I have adopted those found using residual permutation, as they are slightly larger than those from the Monte Carlo results. My final solution is given in Table 2 and compared to those of O’Donovan et al. (2006) and Holman et al. (2007b). As with TrES-1 I find parameter values in good agreement with those from other studies, but my uncertainties are somewhat larger (by factors of up to 3). When studying HD 189733 and HD 209458 (see below) I find that my solutions of different light curves do not agree to within the uncertainties I find. This indicates that my uncertainties are not overestimated, and so that the uncertainties given in previous studies can be quite optimistic. This phenomenon is not peculiar to TrES-2 or the analyses of O’Donovan et al. (2006) and Holman et al. (2007b) but occurs for most of the TEPs studied in this work.

3.3 XO-1

This was discovered to be a TEP by the XO project (McCullough et al. 2006). A light curve was also obtained by SuperWASP-North and is presented by Wilson et al. (2006). The light curves from these two small-aperture large-field instruments are not definitive. Good light curves were obtained and studied by Holman et al. (2006) using a variety of telescopes and passbands.

In this work I have analysed the two best data sets, which come from the FLWO 1.2-m (z band, two transits, 821 data points) and the Palomar 1.5-m (R band, 209 data points) telescopes. I have adopted $P_{\text{orb}} = 3.941534 \, \text{d}$ and a mass ratio of 0.001 (McCullough et al. 2006). The results are given in Table A3 for the FLWO data: the Palomar data set gives substantially larger parameter uncertainties. The solutions with two fitted LDCs give the lowest scatter, and well-defined coefficients (except for the square-root law), so have been used to calculate the final results. As with TrES-1, the best-fitting $\mu_A$ for the linear law does not agree with theoretical predictions. The residual-permutation uncertainties are in good agreement with the Monte Carlo results, indicating that correlated noise is not important for these data.

The quadratic-law best fit is shown in Fig. 5 and the final light-curve parameters are given in Table 3. The agreement between the parameters found here and those of Holman et al. (2006) is excellent, but again my uncertainties are significantly greater. The results of McCullough et al. (2006) and Wilson et al. (2006) also agree well, taking into account the lower quality of the light curves available to them.

3.4 WASP-1

WASP-1 was presented as a candidate TEP by Christian et al. (2006), and its planetary nature was confirmed by Collier Cameron et al. (2007). A decent I-band light curve, containing 583 data points covering two transits, was presented by Shporer et al. (2007). A good z-band light curve was obtained by Charbonneau et al. (2007) and contains 657 data points.

I have analysed both the Shporer and Charbonneau light curves here, adopting $P_{\text{orb}} = 2.519961 \, \text{d}$ and a mass ratio of 0.00075 (Shporer et al. 2007). The results for the Shporer data are given in Table A4: fitting for two LDCs does not cause a significant improvement in the results so I have used the solutions for fitting one LDC. From this point on, solutions with fixed LDCs have not been calculated as they are less reliable than other approaches. This is because the imposition of fixed LDCs is an artificial constraint which can both bias the best fit and decrease the derived parameter uncertainties.

Table 2. Final parameters of the fit to the Holman et al. (2007b) light curve of TrES-2 from the JKTEBOP analysis. These have been compared to the properties of TrES-2 found by O’Donovan et al. (2006) and Holman et al. (2007b). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th>This work</th>
<th>O’Donovan et al. (2006)</th>
<th>Holman et al. (2007b)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_b$</td>
<td>0.1460 ± 0.0042</td>
<td>0.1429</td>
<td>0.1475</td>
</tr>
<tr>
<td>$k$</td>
<td>0.1268 ± 0.0032</td>
<td>0.1273</td>
<td>0.1253 ± 0.0010</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>83.71 ± 0.42</td>
<td>83.90 ± 0.22</td>
<td>83.57 ± 0.14</td>
</tr>
<tr>
<td>$r_A$</td>
<td>0.1296 ± 0.0038</td>
<td>0.1267</td>
<td>0.1311 ± 0.0021</td>
</tr>
<tr>
<td>$r_b$</td>
<td>0.01643 ± 0.00046</td>
<td>0.01614</td>
<td>0.0164 ± 0.0004</td>
</tr>
</tbody>
</table>
Table 3. Final parameters of the fit to the Holman et al. (2007b) light curve of XO-1 from the JKTEBOP analysis. These have been compared to the properties of XO-1 found by McCullough et al. (2006) and Wilson et al. (2006), as well as those of Holman et al. (2006). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_b$</td>
<td>0.1003 ± 0.0022</td>
<td>0.1080</td>
<td>0.1084</td>
<td>0.1000</td>
</tr>
<tr>
<td>$k$</td>
<td>0.1317 ± 0.0019</td>
<td>0.134 ± 0.004</td>
<td>0.138 ± 0.020</td>
<td>0.13102 ± 0.00064</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>89.06 ± 0.84</td>
<td>87.7 ± 1.2</td>
<td>88.9 ± 1.0</td>
<td>89.31 ± 0.46</td>
</tr>
<tr>
<td>$r_A$</td>
<td>0.0886 ± 0.0019</td>
<td>0.0953</td>
<td>0.0953</td>
<td>0.0884</td>
</tr>
<tr>
<td>$r_b$</td>
<td>0.01166 ± 0.00035</td>
<td>0.01273</td>
<td>0.01312</td>
<td>0.01159</td>
</tr>
</tbody>
</table>

Table 4. Final parameters of the fit to the Shporer et al. (2007) and Charbonneau et al. (2007) light curves of WASP-1 from the JKTEBOP analysis. These have been compared to the properties of WASP-1 found by Shporer et al. (2007) and Charbonneau et al. (2007). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th>This work (Shporer data)</th>
<th>This work (final result) (Charbonneau data)</th>
<th>Shporer et al. (2007)</th>
<th>Charbonneau et al. (2007)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_b$</td>
<td>0.200 ± 0.015</td>
<td>0.1918 ± 0.001</td>
<td>0.1909</td>
<td></td>
</tr>
<tr>
<td>$k$</td>
<td>0.1033 ± 0.0016</td>
<td>0.1045 ± 0.0015</td>
<td>0.1015 ± 0.0013</td>
<td>0.1019 ± 0.0009</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>84.0 ± 9.0</td>
<td>86.5 ± 9.0</td>
<td>89.8 ± 1.9</td>
<td>86.1 ± 0.90</td>
</tr>
<tr>
<td>$r_A$</td>
<td>0.182 ± 0.011</td>
<td>0.1737 ± 0.007</td>
<td>0.1733 ± 0.0091</td>
<td></td>
</tr>
<tr>
<td>$r_b$</td>
<td>0.0187 ± 0.0013</td>
<td>0.0182 ± 0.0007</td>
<td>0.0176</td>
<td></td>
</tr>
</tbody>
</table>

The residual-permutation algorithm gives uncertainties which are substantially greater than the Monte Carlo uncertainties: this problem seems to arise because the WASP-1 has a high orbital inclination (low impact parameter) which is therefore poorly constrained. This difficulty also occurs when analysing the Charbonneau light curve (Table A5), and means that $i$ is only constrained to lie between 86° and 90°.

For the final results I adopt my solution of the Charbonneau light curve with parameter uncertainties from the residual-permutation algorithm. The high-inclination nature of this system means its photometric parameters (particularly $i$) are not very well defined despite the availability of high-precision light curves. More extensive high-quality photometric observations are needed for WASP-1. My solution of the Charbonneau light curve is in reasonable agreement with the solution of the Shporer light curve and with the results given by Charbonneau et al. (2007) and Shporer et al. (2007), although the published results have lower uncertainty estimates and slightly smaller ratios of the radii (Table 4). My solutions are compared to the observations in Fig. 6.

3.5 WASP-2

WASP-2 was presented as a TEP candidate by Street et al. (2007) and confirmation of its nature was presented by Collier Cameron et al. (2007). Charbonneau et al. (2007) obtained a good $z$-band light curve (426 data points) which I have analysed here. I adopted $P_{\text{orb}} = 2.152226 \text{ d}$ from Collier Cameron et al. (2007) and a mass ratio of 0.001. In contrast to WASP-1, this system has a lower inclination ($i = 84.8°$) and therefore much better defined fractional radii. This comparison makes it clear that it is much easier to measure the radii of TEPs which do not have central transits.

Table A6 contains the results of the JKTEBOP analysis and demonstrates that allowing two LDCs to be fitted instead of one does not improve the quality of the fit at all and results in very small non-linear LDCs. The residual-permutation method gives very similar uncertainties to the Monte Carlo analysis. For the final results I therefore adopt the solutions with one LDC fitted and with Monte Carlo uncertainties (Table 5) – these results are in reasonable agreement with those of Charbonneau et al. (2007). The best fit is plotted in Fig. 7.

3.6 HAT-P-1

This object was found to be a TEP system by Bakos et al. (2007a) from data taken by the HAT project (Bakos et al. 2002, 2004). Excellent light curves from the FLWO 1.2-m ($z$ band, 1709 observations), Lick 1.0-m ($Z$ band, 1475 data points) and Wise 1.0-m telescopes have been presented and analysed by Winn et al. (2007c).

I have studied the FLWO and Lick observations from Winn et al. (2007c) in this work, adopting a mass ratio of 0.00045 (Bakos et al. 2007a) and including $P_{\text{orb}}$ as one of the fitted parameters. For both data sets the solutions with two fitted LDCs gave no significant improvement over those with one fitted LDC (Tables A7 and A8), so the latter were used to calculate the light-curve results. The residual-shift algorithm uncertainties were adopted as these are larger than the Monte Carlo method. The FLWO and Lick results are in excellent agreement (Table 6, Fig. 8) so they were combined using a weighted mean to obtain the final results. The final result is in good agreement with published analyses, and the photometric properties of HAT-P-1 are very well determined.

3.7 OGLE-TR-10

The transiting nature of this object was discovered by Udalski et al. (2002a) in the course of the OGLE-III project. Konacki et al. (2003b) and Bouchy et al. (2005a) subsequently found a small radial velocity motion, and its exoplanetary status was confirmed by Konacki et al.
Figure 6. Phased light curves of the transits of WASP-1 from Shporer et al. (2007) (grey points) and Charbonneau et al. (2007) (black points) compared to the best fits found using JKTEBOP (red line for the Shporer data and blue line for the Charbonneau data) and the quadratic LD law with the linear LDC included as a fitted parameter. The residuals of the fits are plotted at the bottom of the figures, offset from zero.

Table 5. Final parameters of the fit to the Charbonneau et al. (2007) light curve of WASP-2 from the JKTEBOP analysis. These have been compared to the properties of WASP-2 found by Charbonneau et al. (2007). I have not included the parameters from Collier Cameron et al. (2007) as they are very uncertain due to the larger observational errors in the SuperWASP discovery light curve.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>This work</th>
<th>Charbonneau et al. (2007)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_b$</td>
<td>$0.1409 \pm 0.0067$</td>
<td>$0.1309 \pm 0.0015$</td>
</tr>
<tr>
<td>$k$</td>
<td>$0.1313 \pm 0.0017$</td>
<td>$0.1309 \pm 0.0015$</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>$84.83 \pm 0.53$</td>
<td>$84.74 \pm 0.39$</td>
</tr>
<tr>
<td>$r_A$</td>
<td>$0.1245 \pm 0.0058$</td>
<td>$0.1245 \pm 0.0051$</td>
</tr>
<tr>
<td>$r_b$</td>
<td>$0.01635 \pm 0.00093$</td>
<td>$0.01635 \pm 0.00093$</td>
</tr>
</tbody>
</table>

(2005). It was originally thought to be abnormally large for its radius; improved photometry has removed this anomaly but it remains one of the most bloated of the known TEPs.

Dedicated photometric studies of OGLE-TR-10 have been presented by Holman et al. (2007a) and Pont et al. (2007a). The former study is based on an $I$-band light curve obtained using the Magellan telescope, which fully covers two transits separated by almost 1 yr. The latter study includes $V$- and $R$-band data covering only part of a single transit, observed with the Very Large Telescope (VLT).

Figure 7. Phased light curve of the transit of WASP-2 from Charbonneau et al. (2007) compared to the best fit found using JKTEBOP and the quadratic LD law with the linear LDC included as a fitted parameter. The residuals of the fit are plotted at the bottom of the figure, offset from zero.

The Magellan and VLT observations do not agree on the depth of the transit. This is attributed by Pont et al. (2007a) to systematic errors arising from the use of image subtraction by Holman et al. (2007a). The OGLE data indicate a transit depth of ~1.9 per cent ($I$ band), the Magellan data have a transit depth of 1.1 per cent ($I$ band) and the VLT light-curve transit depth is 1.4 per cent ($V$ and $R$). A version of the OGLE light curve, detrended using the algorithm of Kruszewski & Semeniuk (2003), gives a transit depth in agreement with the VLT data (Pont et al. 2007a).

I have analysed both the Magellan (Holman et al. 2007a) and VLT (Pont et al. 2007a) light curves for OGLE-TR-10, and separate solutions are given for both data sets. A mass ratio of 0.00056 and an initial period of 3.101278 d were adopted (Holman et al. 2007a). For the Magellan data, I have included the period as a fitted parameter. For the VLT data the orbital period is a crucial quantity: because only half of one transit was observed, $P_{orb}$ is very highly correlated with $T_0$ and with $r_A$ and $r_b$. Adopting a fixed $P_{orb}$ and $T_0$ might therefore bias both the resulting $r_A$ and $r_b$ and their error estimates. To avoid these problems I have taken six times of minimum light from the literature (the five times quoted by Holman et al. 2007a and the $T_0$ given by Konacki et al. 2005) and have included $P_{orb}$ and $T_0$ as fitted parameters. JKTEBOP treats both the times of minimum and the light-curve data points as observational data (see Southworth et al. 2007a), allowing an optimal and statistically correct solution to be found. Uncertainties in all observed quantities are included in the Monte Carlo analysis, so the error estimates also take into account the uncertainties in individual times of minimum light.

For the Magellan data the best results were found by fitting for only one LDC (Table A9) and the largest parameter uncertainties were obtained by the residual-shift method – the presence of significant correlated errors is unsurprising given that OGLE-TR-10 is in a crowded stellar field. The best results for the VLT also come from fitting only one LDC, but in these cases the residual-shift method indicates that correlated errors are not important.

The solutions of the two VLT light curves are not in great agreement (Tables A10 and A11), but the differences are less than 1.7σ for
Table 6. Final parameters of the fit to the Winn et al. (2007c) FLWO and Lick light curves of HAT-P-1 from the JKTEBOP analysis, compared to those found by Winn et al. (2007c) and Bakos et al. (2007a). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>This work (FLWO)</th>
<th>This work (Lick)</th>
<th>This work (final)</th>
<th>Bakos et al. (2007a)</th>
<th>Winn et al. (2007d)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_b$</td>
<td>0.1026 ± 0.0037</td>
<td>0.1056 ± 0.0056</td>
<td>0.1035 ± 0.0031</td>
<td>0.1089</td>
<td>0.1044</td>
</tr>
<tr>
<td>$k$</td>
<td>0.1125 ± 0.0011</td>
<td>0.1102 ± 0.0047</td>
<td>0.1124 ± 0.0010</td>
<td>0.122</td>
<td>0.11094 ± 0.00082</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>86.37 ± 0.31</td>
<td>86.10 ± 0.38</td>
<td>86.26 ± 0.24</td>
<td>85.9 ± 0.8</td>
<td>86.22 ± 0.24</td>
</tr>
<tr>
<td>$r_A$</td>
<td>0.0922 ± 0.0033</td>
<td>0.0951 ± 0.0053</td>
<td>0.0930 ± 0.0028</td>
<td>0.0971</td>
<td>0.0940 ± 0.0028</td>
</tr>
<tr>
<td>$r_b$</td>
<td>0.01037 ± 0.00046</td>
<td>0.01048 ± 0.00047</td>
<td>0.01043 ± 0.00033</td>
<td>0.0118</td>
<td>0.0104 ± 0.0004</td>
</tr>
</tbody>
</table>

Figure 8. Phased light curves of the transit of HAT-P-1 from Winn et al. (2007c) compared to the best fits found using JKTEBOP and the quadratic LD law. The FLWO $z$-band data are plotted at the top and the Lick Z-band light curve is offset by −0.02. The residuals of the fit are plotted at the bottom of the figure, offset from zero.

For each parameter, I have taken a weighted mean of the VLT $V$ and $R$ light-curve solutions, with uncertainties slightly increased to take into account the differences. This solution does not agree well with the Magellan data, as was also found by Pont et al. (2007a). The best fits are plotted in Fig. 9, where it can be seen that the two VLT light curves give noticeably different solutions, but both have clearly deeper transits than the Magellan data. The residuals of the best fit confirm that in each case the model provides a good representation of the observations, so any discrepancies are due to the data themselves.

The agreement between our final solution (based on the VLT $V$ and $R$ data) and published analyses is not good (Table 7). The results of Konacki et al. (2005) were based on the low-precision OGLE photometry, so it is not surprising that these disagree with later analyses. Those of Holman et al. (2007a) are in acceptable agreement with our own solution of the Magellan data, whereas the results from Pont et al. (2007a) are not in accord with our analysis.

Whilst the solution of the VLT data found here should be robust, OGLE-TR-10 would clearly benefit from further photometric study.

3.8 OGLE-TR-56

This object was the second TEP discovered, and the first using the extensive photometric data base built up by OGLE. Its eclipsing nature was discovered by Udalski et al. (2002b) and it was confirmed to be a planet by Konacki et al. (2003a) from Keck radial velocity observations. Further radial velocities, and re-analyses of the OGLE light curve, have been presented by Torres et al. (2004) and Bouchy et al. (2005a).
Aside from the survey-quality photometry obtained by OGLE, the only light curves of OGLE-TR-56 were obtained by Pont et al. (2007a). Observations covering one full transit were taken in the V and R passbands using the VLT and FORS1 (Focal Reducer/low dispersion Spectrograph 1) instrument. The two light curves have a very good photometric precision, particularly considering the apparent magnitude of OGLE-TR-56, but only a small number of data points. I have studied these two light curves, graciously provided by F. Pont, using $P_{\text{orb}} = 1.211909 \, \text{d}$ and a mass ratio of 0.001 (Pont et al. 2007a).

For both light curves, solutions with both LDCs free gave poor results (see Tables A12 and A13). The final results have therefore been taken from the solutions with the linear LDC free and the non-linear one fixed at theoretically expected values (and perturbed during the Monte Carlo analysis). For both data sets the residual-shift algorithm gave similar results to the Monte Carlo, indicating that correlated errors are not important. For the R-band data the solution with the linear LD law is unphysical ($u_A > 1.0$) – the LDC must be fixed when solving this light curve. In addition, the logarithmic and cubic LD law solutions are discrepant so have not been included in the final solution.

The best fits to the two VLT light curves are shown in Fig. 10; the two fits are not visually in good agreement. This can be seen in the final fits to each data set given in Table 8, but the two solutions are actually consistent when the sizes of the error bars are taken into account. I have therefore used the weighted average of the two for the final solution for OGLE-TR-56 (Table 8). A comparison with published results for this TEP shows reasonable agreement when the quality of the OGLE data is taken into account. This system would benefit from more extensive photometry.

### 3.9 OGLE-TR-111

This was also found to be transiting by OGLE (Udalski et al. 2002c) and has a low density. Its TEP nature was confirmed by Pont et al. (2004) and light-curve studies have been published by Minniti et al. (2007) and Winn, Holman & Fuentes (2007a). The data set obtained by Winn et al. (2007a) is the best and is easily available so was chosen for analysis. It was obtained in the (presumably Cousins) I band and contains 386 observations. I adopted $P_{\text{orb}} = 4.0144479 \, \text{d}$ and a mass ratio of 0.0007 (Winn et al. 2007a) (remember that the value of the mass ratio has extremely little influence on the light-curve solutions).

As for OGLE-TR-10 and OGLE-TR-56 no substantial gain was found in fitting for both LDCs (Table A14), so the non-linear LDC was fixed for the final solution (and perturbed as usual during the error analysis). The residual-shift method gave slightly larger uncertainties, so correlated errors are important for these data. The final results are given in Table 9 and plotted in Fig. 11, and show good agreement with the study by Winn et al. (2007a).

### 3.10 OGLE-TR-132

OGLE-TR-132 was originally discovered as a candidate transiting system by Udalski et al. (2003) and confirmed to be a TEP by Bouchez et al. (2004). A light curve from the VLT was presented by Moutou et al. (2004). The data were re-analysed using image deconvolution by Gillon et al. (2007a), who found that the previous light curve was affected by systematic errors from the data reduction. An excellent discussion and examples of this problem are given by Gillon et al.
ment between the different solution sets. The orbital inclination is

\[ i = 20.0 \pm 0.2 \text{ degrees} \]

\[ \rho = 0.0009 \text{ (Gillon et al. 2007a).} \]

Correlated noise more important. I adopted a period of 1.689868 d

Table 8. Final parameters of the fit to the Pont et al. (2007a) light curves of OGLE-TR-56 from the JKTEBOP analysis. These have been compared to the properties of the system found by Konacki et al. (2003a), Torres et al. (2004), Bouchy et al. (2005a) and Pont et al. (2007a). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th>This work (V)</th>
<th>This work (R)</th>
<th>This work (final)</th>
<th>Konacki et al. (2003a)</th>
<th>Torres et al. (2004)</th>
<th>Bouchy et al. (2005a)</th>
<th>Pont et al. (2007a)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r_A + r_b )</td>
<td>0.275 ± 0.038</td>
<td>0.259 ± 0.048</td>
<td>0.269 ± 0.030</td>
<td>0.255</td>
<td>0.242</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( k )</td>
<td>0.1014 ± 0.006</td>
<td>0.0907 ± 0.0116</td>
<td>0.0991 ± 0.0054</td>
<td>0.121</td>
<td>0.124</td>
<td>0.114 ± 0.004</td>
<td>0.101 ± 0.002</td>
</tr>
<tr>
<td>( i (\text{deg}) )</td>
<td>78.8 ± 3.0</td>
<td>81.8 ± 4.1</td>
<td>79.8 ± 2.4</td>
<td>86 ± 2</td>
<td>81.0 ± 2.2</td>
<td>81 to 90</td>
<td>0.26 ± 0.01</td>
</tr>
<tr>
<td>( r_A )</td>
<td>0.250 ± 0.034</td>
<td>0.237 ± 0.041</td>
<td>0.245 ± 0.026</td>
<td>0.227</td>
<td>0.215</td>
<td>0.268</td>
<td></td>
</tr>
<tr>
<td>( r_b )</td>
<td>0.0253 ± 0.0041</td>
<td>0.0215 ± 0.0062</td>
<td>0.0241 ± 0.0034</td>
<td>0.0276</td>
<td></td>
<td>0.0268</td>
<td></td>
</tr>
</tbody>
</table>

Table 9. Final parameters of the fit to the Winn et al. (2007a) light curve of OGLE-TR-111 from the JKTEBOP analysis. These have been compared to the properties of OGLE-TR-111 found by Pont et al. (2004), Winn et al. (2007a) (from the same data as analysed here) and Minniti et al. (2007).

<table>
<thead>
<tr>
<th></th>
<th>This work</th>
<th>Pont et al. (2004)</th>
<th>Winn et al. (2007a)</th>
<th>Minniti et al. (2007)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r_A + r_b )</td>
<td>0.0952 ± 0.0044</td>
<td>0.0943</td>
<td>0.09288</td>
<td></td>
</tr>
<tr>
<td>( k )</td>
<td>0.1316 ± 0.0023</td>
<td>0.1209</td>
<td>0.132 ± 0.002</td>
<td>0.1245 ± 0.0030</td>
</tr>
<tr>
<td>( i (\text{deg}) )</td>
<td>88.11 ± 0.66</td>
<td>86.5 to 90.0</td>
<td>88.1 ± 0.3</td>
<td>87.0 to 90.0</td>
</tr>
<tr>
<td>( r_A )</td>
<td>0.0842 ± 0.0038</td>
<td>0.0841</td>
<td>0.0926 ± 0.006</td>
<td>0.1028</td>
</tr>
<tr>
<td>( r_b )</td>
<td>0.01107 ± 0.00067</td>
<td>0.01017</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 11. Phased light curve of the transits of OGLE-TR-111 from Winn et al. (2007a) compared to the best fit found using JKTEBOP and the quadratic LD law with the linear LDC included as a fitted parameter. The residuals of the fit are plotted at the bottom of the figure, offset from zero.

I have solved the VLT light curve from Gillon et al. (2007a) (274 observations), which have good precision but do not quite cover the full transit, finishing immediately before the point of fourth contact. Unfortunately, this lowers the accuracy of the results, and makes correlated noise more important. I adopted a period of 1.689868 d and a mass ratio of 0.0009 (Gillon et al. 2007a).

Solutions with two fitted LDCs gave poorly defined coefficients (Table A15) so I have adopted the results of the solutions with the non-linear LDC fixed. The values of \( r_A \) and \( r_b \) are in good agreement between the different solution sets. The orbital inclination is not measured very accurately, and it is important to obtain a new light curve which fully covers the transit. The largest parameter uncertainties are found by the residual-shift method, and this is probably because the light curve does not fully cover the transit. Table 10 contains the final parameters and the best-fitting model is plotted in Fig. 12.

Table 10. Final parameters of the fit to the Gillon et al. (2007a) light curve of OGLE-TR-132 from the JKTEBOP analysis. These have been compared to the properties of OGLE-TR-132 found by Moutou et al. (2004) and Gillon et al. (2007a). Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th>This work</th>
<th>Moutou et al. (2004)</th>
<th>Gillon et al. (2007c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r_A + r_b )</td>
<td>0.231 ± 0.023</td>
<td>0.0937 ± 0.0026</td>
<td>0.0812 ± 0.0017</td>
</tr>
<tr>
<td>( k )</td>
<td>0.9937 ± 0.0026</td>
<td>0.0812 ± 0.0017</td>
<td>0.0916 ± 0.0014</td>
</tr>
<tr>
<td>( i (\text{deg}) )</td>
<td>83.3 ± 2.4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( r_A )</td>
<td>0.211 ± 0.020</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( r_b )</td>
<td>0.0198 ± 0.0024</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3.11 GJ 436

The M dwarf system GJ 436 is a unique object among the known TEPs as both the planet and star are by far the smallest and least massive; the system also has a currently unexplained eccentric orbit. This was known to be a planetary system from spectroscopic radial velocity measurements (Butler et al. 2004; Maness et al. 2007) and transits were first detected by Gillon et al. (2007c). A good light curve of the transit has been obtained using the Spitzer Space Telescope (Deming et al. 2007a; Gillon et al. 2007b). Spitzer has also been used to study the secondary eclipse (Deming et al. 2007a; Demory et al. 2007). Torres (2007) has measured the parameters of the system from its light and radial velocity curves, theoretical stellar models and
its measured absolute $K$-band magnitude and $J - K$ colour index. He found that the star has a radius inflated by approximately 10 per cent over that predicted by the models, an anomaly which has previously been noticed for low-mass stars in eclipsing binary systems (Ribas 2003, 2006; López-Morales 2007), single low-mass field stars studied using interferometry (Berger et al. 2006) and the low-mass secondary components of interacting binaries (Littlefair et al. 2006).

I have chosen to analyse the Spitzer light curve presented by Gillon et al. (2007b), which contains 355 data points covering one transit at a wavelength of 8 μm. It is not possible to constrain the orbital eccentricity and longitude ofperiastron, $e$ and $\omega$, from one transit so I have adopted the values $e = 0.14 \pm 0.01$ (Demoruy et al. 2007) and $\omega = 351^\circ \pm 1.2^\circ$ (Maness et al. 2007). I have also taken $P_{\text{orb}} = 2.64385$ d from Gillon et al. (2007b) and a mass ratio of 0.00016 from Torres (2007). An additional complication is that the brightness of the planet is not negligible at 8 μm. From Deming et al. (2007a, figs 1 and 2) I find a surface brightness ratio of approximately 7 per cent. The surface brightness ratio has been fixed at this value; changes of a factor of 2 have a smaller effect on the radii than the final error bars. Similarly, changes of $e$ and $\omega$ within their quoted error bars have a negligible effect on the final results.

Attempts to fit for LD did not lead to realistic results (Table A16). Whilst the photometry achieves a remarkable precision (0.7 mmag per point), the observational scatter is still a significant fraction of the very shallow transit depth. The Spitzer data are taken at 8 μm where the effect of LD is minor, so for the final solutions it was acceptable to fix the LDCs to predicted values. The effects of correlated noise are not important. The final results are given in Table 11 and shown in Fig. 13. The agreement with literature values is good, but the solution does not lead to particularly accurate radii for either star or planet. Improved photometry is needed, and may be provided in the near future by the Transit Light Curve project (see Winn 2007).

3.12 HD 149026

HD 149026b is a very anomalous object, with one of the highest densities of the known TEPs. Its small size suggests that much of its mass lies in a rock/ice core, and HD 149026 has been the subject of several theoretical investigations concerning its formation and chemical composition (e.g. Johnson, Goodman & Menou 2006; Broeg & Wuchterl 2007; Matsuo et al. 2007; Zhou & Lin 2007).

The TEP nature of HD 149026 was discovered by Sato et al. (2005), and light curves have also been presented by Charbonneau et al. (2006) from the FLWO 1.2-m telescope. However, the very shallow transit (depth 0.3 per cent) means that its light-curve parameters remain ill defined despite the reasonably good quality of the available photometry. Wolf et al. (2007) have studied the Rossiter–McLaughlin effect in the system and Bozorgnia et al. (2006) have searched for the presence of lithium and potassium in the planetary atmosphere. Harrington et al. (2007) observed a secondary eclipse of HD 149026 with Spitzer and found a high brightness temperature at 8 μm of 2300 ± 200 K for the planet.

In this work I have solved the $(b + y)/2$ light curve from Sato et al. (2005) and the $g$- and $r$-band data from Charbonneau et al. (2006). My initial solutions converged to values for the orbital inclination of either $i \approx 81^\circ$ or $\approx 90^\circ$. To investigate this, additional solutions were calculated with $i$ fixed to values between 90° and 70° in steps of 0.2°. The quality of the fit for these additional solutions is shown in Fig. 14, and the results for the three light curves are not in good agreement with each other or with the analogous diagram presented by Sato et al. (2005, their fig. 5).

The solutions for the $g$ light curve were very poorly behaved: standard approaches tended to go to an ill-defined solution with $i \approx 81^\circ$, but the additional solutions did not reproduce the corresponding fit parameters even when $i$ was fixed at values near 81°. This indicates that the $\chi^2$ surface in parameter space has substantial structure, and these data have not been considered further.

The solutions for the $r$ and $(b + y)/2$ light curves are better behaved and the resulting parameters are in reasonable agreement (even though the best fits are not; see Fig. 15). The $(b + y)/2$ light curve is the best data set, and it was possible to obtain meaningful values for the linear LDCs when the non-linear LDCs were fixed. These solutions were therefore adopted as the final results for the $(b + y)/2$ data. Analyses of the $r$ light curve tended to give unphysical LDCs, so these had to be fixed at theoretically predicted values for the final solutions of these data. Attempts to fit for both LDCs for either light curve resulted in an impressive variety of physically impossible solutions.

The nature of the transit of HD 149026 means that the inclination remains very poorly constrained. This uncertainty over which part of the stellar disc the planet eclipses causes the fractional radii of

\[ r_i = 0.0016 \pm 0.0001 \]

\[ r_o = 0.0016 \pm 0.0001 \]

\[ i = 89.9 \pm 0.1 \]

\[ i = 90.0 \]

Some of the Monte Carlo simulation results presented by Charbonneau et al. (2006, their fig. 2) are concentrated in a sharp peak at $i \approx 90^\circ$ whilst most of the results occupy a much broader distribution at $i \approx 86^\circ$. A probably similar effect was seen whilst writing the Monte Carlo algorithm for JKTEBOP and is caused by the value of $i$ becoming almost exactly 90° during the model fitting process. When this happens a numerical derivative will vanish (or an alternative solution will not be taken) if it is calculated symmetrically, because the symmetrical nature of the situation means that a solution with e.g. $i = 89.9$ is equivalent to $i = 90.1$. Thus the fit becomes stuck at $i = 90^\circ$ without physical justification. This effect can be avoided by not allowing $i > 90^\circ$. Charbonneau et al. (2006) correctly identify their sharp peak at $i \approx 90^\circ$ as a numerical problem and do not use the relevant simulations, so their results will be unaffected.
Table 11. Final parameters of the fit to the Spitzer light curve of GJ 436 from the JKTEBOP analysis, compared to those found by other authors. Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th>This work</th>
<th>Gillon et al. (2007b)</th>
<th>Gillon et al. (2007c)</th>
<th>Deming et al. (2007a)</th>
<th>Torres (2007)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_b$</td>
<td>0.0791 ± 0.0029</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$k$</td>
<td>0.08284 ± 0.00090</td>
<td>0.082 ± 0.005</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>86.43 ± 0.18</td>
<td>86.5 ± 0.2</td>
<td>85.90^19.19</td>
<td></td>
<td>0.0758 ± 0.0035</td>
</tr>
<tr>
<td>$r_A$</td>
<td>0.0731 ± 0.0027</td>
<td>0.0758 ± 0.0035</td>
<td>0.0750 ± 0.0033</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$r_b$</td>
<td>0.00605 ± 0.00023</td>
<td>0.00634</td>
<td>0.00626</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 13. Phased light curve of the transit of GJ 436 from Spitzer compared to the best fit found using JKTEBOP and the quadratic LD law with both LDCs included as fitted parameters. The residuals of the fit are plotted at the bottom of the figure, offset from zero.

both components to be ill defined, and the upper and lower confidence intervals for individual measurements are quite unbalanced. I have adopted the Charbonneau $r$ outcome as the final results for HD 149026 (Table 12), but have increased the error estimates to reflect the difference between the $r$ and $(b + y)/2$ solutions. This choice results in more precise parameter values, compared to the $(b + y)/2$ solution, but is dependent on theoretically derived LDCs. However, any systematic error arising from the use of theoretical LDCs should be much smaller than the random errors of the current solution.

The final solution presented here is not in good agreement with the $i$, $r_A$ and $r_b$ values found in previous studies (Sato et al. 2005; Charbonneau et al. 2006; Wolf et al. 2007). It corresponds to a higher (but still poorly defined) $i$, which means smaller $r_A$ and $r_b$ values are needed to give a transit of the observed duration. The substantially smaller $r_b$ found here indicates that the planet in the HD 149026 system has an even larger density than previously thought. The only reasonable conclusion that can be drawn is that better light curves are needed before we can attain a precise understanding of the HD 149026 system.

After the above analysis was performed, another study of HD 149026 became available. Winn et al. (2008) have obtained new photometry and arrive at a high-$i$ solution which is in good agreement with my own results. The fractional radii of the star and planet are still not well defined, so additional high-precision photometry remains a priority for observers.

3.13 HD 189733

HD 189733 was found to be a TEP by Bouchy et al. (2005b) and is now one of the best-studied systems due to its brightness and relatively deep transit. It has a faint stellar companion separated by 11.2 arcsec on the sky (Bakos et al. 2006a). HD 189733 A has a detectable magnetic field (Moutou et al. 2007) so is an interesting target for studying the activity of planet host stars. A rotational period of 11.953 ± 0.009 d was determined by Henry & Winn (2008) from photometry of its star-spot-induced brightness modulation. Hébrard...
primary and secondary minima have also been studied from space
studied by Bakos et al. (2006b) and Winn et al. (2006, 2007a). The
needed.
are clear through the partial eclipse phases, and show that better data are
The differences between the best-fitting solutions for the three light curves
All three data sets have been binned by a factor of 5 for display purposes.
residuals of the fit are plotted at the bottom of the figure, offset from zero.
et al. (2005) LCs all LDCs were fixed at theoretically expected values. The
et al. (2005) data the linear LDC was fitted for whereas for the Charbonneau
to the best fit found using JKTEBOP and the quadratic LD law. For the Sato
Phased light curves of the transits of HD 149026 from Sato et al.
& Lecavelier Des Etangs (2006) found eclipses in its Hipparcos light
Ground-based photometry of HD 189733 has been presented and
Deming et al. 2006; Knutson et al. 2007c) but such a small value has a negligible effect on the parameters derived in this work. I have taken $P_{\text{orb}} = 2.2185733$ d from Winn et al. (2006) and a mass ratio of 0.0014 from Winn et al. (2006).
For each of the light curves it was difficult to extract reliable val-
ues for both LDCs so I have adopted the solutions with one LDC
fixed (Tables A18, A19 and A20). The Monte Carlo and residual-
permutation uncertainties were similar so correlated noise is not
important for these data sets. The best-fitting light curves are com-
pared with the data in Fig. 16.
The solutions of the three light curves are inconsistent (Table 13),
due mainly to a mismatch of 6.7σ in the ratio of the radii, $k$. This
results in discrepancies of 3.1σ in $r_A$ and 2.1σ in $r_B$. As $k$ depends
essentially on the eclipse depth, this problem is related to the data
rather than to the analysis. It is not very surprising that this
discrepancy exists, because obtaining light curves of TEPs is an ob-
servationally demanding activity. An example of systematic prob-
lems with the eclipse depth in OGLE-TR-132 was presented and
discussed by Gillon et al. (2007a). For HD 189733 there are three
high-precision light curves available, so the effects of systematic
errors can be estimated in detail. HD 189733 is therefore one of the
best understood of the TEPs. A rather unhappy implication of this
discrepancy is that we can only fully understand the intrinsic props-
erties of a TEP if three independent light curves are available. It is
possible that the presence of star-spots contributes to the different
$k$ values found for the light curves; this could be investigated using
the excellent HST light curve which has since been presented by
Pont et al. (2007b).
For the final solution I have calculated the weighted mean for each
parameter from the three light curves studied here, and have
increased the uncertainties to account for the discrepancies dis-
cussed above. Because of this, the resulting solution is very robust.
More pieces of the jigsaw can be added to this study in the near
future by including the forthcoming HST and MOST data sets. The
study of systematic biases in light-curve parameters is a vital part
of understanding the extent of our knowledge of the properties of
TEPs.

Figure 15. Phased light curves of the transits of HD 149026 from Sato et al. (2005) (top) and Charbonneau et al. (2006) (g middle, r lower) compared to the best fit found using JKTEBOP and the quadratic LD law. For the Sato et al. (2005) data the linear LDC was fitted for whereas for the Charbonneau et al. (2006) LCs all LDCs were fixed at theoretically expected values. The residuals of the fit are plotted at the bottom of the figure, offset from zero. All three data sets have been binned by a factor of 5 for display purposes. The differences between the best-fitting solutions for the three light curves are clear through the partial eclipse phases, and show that better data are needed.

Table 12. Final parameters of the fit to the Sato et al. (2005) and Charbonneau et al. (2006) light curves of HD 149026 from the JKTEBOP analysis. These have been compared to the properties of HD 149026 found by these authors. Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>This work (Sato data)</th>
<th>This work (FLWO g data)</th>
<th>This work (FLWO r data)</th>
<th>This work (final)</th>
<th>Sato et al. (2005)</th>
<th>Charbonneau et al. (2006)</th>
<th>Wolf et al. (2007)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_B$</td>
<td>$0.144^{+0.014}_{-0.011}$</td>
<td>$0.158^{+0.010}_{-0.005}$</td>
<td>$0.147^{+0.011}_{-0.005}$</td>
<td>$0.147^{+0.014}_{-0.008}$</td>
<td>0.169</td>
<td>0.152</td>
<td>0.149</td>
</tr>
<tr>
<td>$k$</td>
<td>$0.047^{+0.005}_{-0.002}$</td>
<td>$0.053^{+0.002}_{-0.003}$</td>
<td>$0.048^{+0.003}_{-0.003}$</td>
<td>$0.046^{+0.006}_{-0.004}$</td>
<td>0.0514</td>
<td>0.0507 ± 0.0015</td>
<td>0.0514</td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>$83.0\text{ to }90.0$</td>
<td>$86.0\text{ to }90.0$</td>
<td>$87.0\text{ to }90.0$</td>
<td>$86.0\text{ to }90.0$</td>
<td>$85.3\pm 1.0$</td>
<td>$85.8^{+1.6}_{-1.3}$</td>
<td>$86.1\pm 1.4$</td>
</tr>
<tr>
<td>$r_A$</td>
<td>$0.138^{+0.061}_{-0.013}$</td>
<td>$0.150^{+0.009}_{-0.005}$</td>
<td>$0.140^{+0.010}_{-0.004}$</td>
<td>$0.140^{+0.012}_{-0.006}$</td>
<td>0.161</td>
<td>0.161</td>
<td>0.161</td>
</tr>
<tr>
<td>$r_B$</td>
<td>$0.0065^{+0.0039}_{-0.0008}$</td>
<td>$0.0089^{+0.0007}_{-0.0004}$</td>
<td>$0.0068^{+0.0008}_{-0.0005}$</td>
<td>$0.0068^{+0.0011}_{-0.0008}$</td>
<td>0.0082</td>
<td>0.0083</td>
<td>0.0083</td>
</tr>
</tbody>
</table>
tially successful (Snellen 2005; Deming, Richardson & Harrington 2007b). Spectroscopic observations of the Rossiter–McLaughlin effect through transit have added to the understanding of HD 209458 (Queloz et al. 2000; Winn et al. 2005; Wittenmyer et al. 2005) and no less than three works have obtained precise $P_{\text{orb}}$ measurements using Hipparcos data (Söderhjelm 1999; Castellano et al. 2000; Robichon & Arenou 2000).

Given such a large amount of data, I have decided to analyse both sets of HST light curves (Brown et al. 2001; Knutson et al. 2007b) and the MOST light curve (Rowe et al. 2006). Studying these data sets allows careful cross-checks of the success of the different solutions and the interagreement of the results, and so indicate whether or not systematic errors (arising particularly from red noise) are important. This is particularly relevant in light of the results for HD 189733 presented above. The HST data of Brown et al. (2001) have been previously solved using JKTEBOP (Southworth et al. 2007b) but are revisited here in order to ensure homogeneity of the results. I have adopted $P_{\text{orb}} = 3.52474859$ d and a mass ratio of 0.00056 from Knutson et al. (2007b).

The HST data obtained by Brown et al. (2001) (556 data points) give good values for both LDCs when the non-linear LD laws are used (Table A21), so these solutions have been adopted. The high quality and relatively blue passband of these data allow the linear LD law to be ruled out at a high significance level (greater than 99.99 per cent). There is less to choose between the non-linear laws, except that the quadratic law gives marginally the best fit. The low Poisson noise means that correlated errors dominate here, so I have adopted the uncertainties from the residual-shift algorithm.

When analysing the MOST data (Rowe et al. 2006) I rejected the data points which were distant from transit (Fig. 17) as these add nothing to the solution except increased computational requirements. I also did not consider data from the second of the four transits as only part of this eclipse was observed. This left a total of 8772 data points. Solutions with two fitted LDCs were not great so I have adopted those with one fitted LDC. As with the HST data, correlated noise is important so I have adopted the uncertainties from the residual-shift algorithm.

### 3.14 HD 209458

In clear contrast to its position as the final object considered in this work, HD 209458 was the first known TEP, with discovery light curves published by Charbonneau et al. (2000) and Henry et al. (2000). It has since become the most heavily studied, and the observational data available for this system constitute an embarrassment of riches. Transit light curves have been obtained by HST (twice; Brown et al. 2001; Knutson et al. 2007b), MOST (Rowe et al. 2006; Croll et al. 2007a), Spitzer (Richardson et al. 2006) and from terrestrial facilities (Wittenmyer et al. 2005). Secondary eclipses have been obtained by Spitzer (Deming et al. 2005; Knutson et al. 2007d) but ground-based attempts have been only partly successful (Snellen 2005; Deming, Richardson & Harrington 2007b). Spectroscopic observations of the Rossiter–McLaughlin effect through transit have added to the understanding of HD 209458 (Queloz et al. 2000; Winn et al. 2005; Wittenmyer et al. 2005) and no less than three works have obtained precise $P_{\text{orb}}$ measurements using Hipparcos data (Söderhjelm 1999; Castellano et al. 2000; Robichon & Arenou 2000).

Given such a large amount of data, I have decided to analyse both sets of HST light curves (Brown et al. 2001; Knutson et al. 2007b) and the MOST light curve (Rowe et al. 2006). Studying these data sets allows careful cross-checks of the success of the different solutions and the interagreement of the results, and so indicate whether or not systematic errors (arising particularly from red noise) are important. This is particularly relevant in light of the results for HD 189733 presented above. The HST data of Brown et al. (2001) have been previously solved using JKTEBOP (Southworth et al. 2007b) but are revisited here in order to ensure homogeneity of the results. I have adopted $P_{\text{orb}} = 3.52474859$ d and a mass ratio of 0.00056 from Knutson et al. (2007b).

The HST data obtained by Brown et al. (2001) (556 data points) give good values for both LDCs when the non-linear LD laws are used (Table A21), so these solutions have been adopted. The high quality and relatively blue passband of these data allow the linear LD law to be ruled out at a high significance level (greater than 99.99 per cent). There is less to choose between the non-linear laws, except that the quadratic law gives marginally the best fit. The low Poisson noise means that correlated errors dominate here, so I have adopted the uncertainties from the residual-shift algorithm.

When analysing the MOST data (Rowe et al. 2006) I rejected the data points which were distant from transit (Fig. 17) as these add nothing to the solution except increased computational requirements. I also did not consider data from the second of the four transits as only part of this eclipse was observed. This left a total of 8772 data points. Solutions with two fitted LDCs were not great so I have adopted those with one fitted LDC. As with the HST data, correlated noise is important so I have adopted the uncertainties from the residual-shift algorithm.

#### 3.14.1 HST observations of Knutson et al. (2007b)

The beautiful HST observations obtained by Knutson et al. (2007b) allow the properties of the HD 209458 system to be determined to a very high precision. These data comprise two separate sets of observations obtained with a blue (504 epochs) and a red grating (548 epochs) using HST/STIS. Each set has been split into five different light curves, resulting in 10 separate light curves evenly distributed between 320 and 980 nm. The variation of LD strength with wavelength is clear and can be a strong test of the predictions of stellar model atmospheres.

### Table 13. Final parameters of the fits to the Bakos et al. (2006b) (FLWO r) and Winn et al. (2007a) (FLWO z and WISE i) light curves of HD 189733 from the JKTEBOP analysis. These have been compared to the properties of HD 189733 found by other workers. Quantities without quoted uncertainties were not given by those authors but have been calculated from other parameters that were.

<table>
<thead>
<tr>
<th></th>
<th>This work (FLWO r data)</th>
<th>This work (FLWO z data)</th>
<th>This work (WISE i data)</th>
<th>This work (final result)</th>
<th>Bouchy et al. (2005b)</th>
<th>Bakos et al. (2006b)</th>
<th>Winn et al. (2007d)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_A + r_B$</td>
<td>0.1184 ± 0.0022</td>
<td>0.1297 ± 0.0023</td>
<td>0.1326 ± 0.0083</td>
<td>0.1287 ± 0.0036</td>
<td>0.1311</td>
<td>0.1301</td>
<td></td>
</tr>
<tr>
<td>$k$</td>
<td>0.1542 ± 0.0019</td>
<td>0.1577 ± 0.0010</td>
<td>0.1499 ± 0.0029</td>
<td>0.1568 ± 0.0024</td>
<td>0.172 ± 0.003</td>
<td>0.1574</td>
<td></td>
</tr>
<tr>
<td>$i$ (°)</td>
<td>86.50 ± 0.59</td>
<td>85.73 ± 0.20</td>
<td>85.38 ± 0.68</td>
<td>85.78 ± 0.25</td>
<td>85.3 ± 0.11</td>
<td>85.79 ± 0.24</td>
<td>85.76 ± 0.29</td>
</tr>
<tr>
<td>$r_A$</td>
<td>0.1026 ± 0.0054</td>
<td>0.1121 ± 0.0019</td>
<td>0.1153 ± 0.0071</td>
<td>0.1113 ± 0.0031</td>
<td>0.1118</td>
<td>0.1124 ± 0.0034</td>
<td></td>
</tr>
<tr>
<td>$r_B$</td>
<td>0.0158 ± 0.0012</td>
<td>0.0177 ± 0.0004</td>
<td>0.0173 ± 0.0012</td>
<td>0.0175 ± 0.0005</td>
<td>0.0192</td>
<td>0.0177 ± 0.0007</td>
<td></td>
</tr>
</tbody>
</table>

The 10 light curves have been solved separated using linear and quadratic LD (Tables A23 and A24), and the best fits and residuals are plotted in Fig. 18. The light curves have a low photon noise so the residual-shift algorithm gives the largest uncertainties. As with the \textit{HST} observations of Brown et al. (2001), the linear LD law gives a significantly worse fit than the quadratic LD law for the bluer wavelength bands. In particular, the referee has correctly pointed out that, for the linear-law case, the orbital inclination values are correlated with the wavelength of observation. This is clearly unphysical and arises from the inadequacy of the linear law being more important at shorter wavelengths where LD is stronger. No correlation is seen for the quadratic-law case.

The variation with wavelength of the linear LDC is compared in Fig. 19 to predictions for the SDSS \textit{ugriz} passbands from Claret (2004). The disagreement between observation and theory is clear. However, detailed conclusions should not be drawn from Fig. 19 for two reasons: the linear law is not a good representation of the LD of stellar discs, and this is more important at bluer wavelengths; and the plotted LDCs are not monochromatic but refer to different passbands. I find that the dependence of the light-curve solutions on wavelength, noted in the previous paragraph, does not have a significant effect on the conclusions drawn from Fig. 19.

In Fig. 20 the observed and predicted LDCs are compared for the quadratic law. The observed LDCs again do not agree with the predicted ones, but investigation of this effect is beyond the scope of the current paper. One interesting point is that the non-linear LDC for the quadratic law dips below zero at the shortest wavelengths,
an effect which is not present in any of the LDC predictions used in this work.

When combining the parameter values obtained for each of the 10 Knutson light curves, their scatter was much larger than the derived uncertainties. The scatter is again relatively the largest for $k$ (11.3σ for the solutions with linear LD and 5.6σ for those with quadratic LD) so for the final result I adopt a weighted mean with uncertainties increased to reflect this greater scatter. Note that this effect is expected because the individual light curves are not independent (they come from the same set of observations). This does not necessarily imply that there are any problems with the observations or the analysis for the quadratic-law case, but the much worse agreement for linear LD does indicate that this function is a poor representation of reality.

I have investigated how the accuracy of the radius measurements varies with wavelength, and find (after compensating for the variation in the precision of the data) that the precision at the reddest wavelengths is roughly twice as good as at the bluest. The quality of the LDC determinations does not change much, but their importance to $r_A$ and $r_b$ decreases with increasing wavelength. This is in agreement with the general belief that redder passbands give more precise results because the effect of LD is less important.

### 3.14.2 Final results for HD 209458

The results of the three light-curve analyses for HD 209458 are given in Table 14 and are not in good agreement. There is again a difference between the results which is larger than expected given the derived errors. This is worst for the ratio of the radii (3.3σ) but surprisingly does not affect $r_A$ or $r_b$ (0.5σ). The fact that the discrepancy remains the worst for $k$ is disquieting because this should be very well determined from the observed eclipse depths. Our understanding of HD 209458 is good, like HD 189733, because sufficient independent data exist for us to make a useful estimate of the importance of systematic errors.

For the final result I have again adopted a weighted mean of the parameters from the three separate light curves but increased the uncertainties to account for the discrepancy between the measurements. The final parameters found here are in reasonable agreement with most literature values. The orbital inclinations found in some published studies are not in good agreement within the errors; this can be attributed to those studies fixing LDCs at theoretical values and so ending up with biased best-fitting parameters and underestimated error bars.

### 4 SURFACE GRAVITIES OF EACH SYSTEM

Southworth et al. (2004c) showed that it is possible to measure the surface gravity of the secondary component of an eclipsing system from only the results of a light-curve analysis and the measured velocity amplitude of the primary component. A simplified formula was given by Southworth et al. (2007b):

$$g_b = \frac{2\pi}{P_{\text{orb}}} \left(1 - e^2\right)^{1/2} \frac{K_\lambda}{r_b^2 \sin i},$$

where $K_\lambda$ is the stellar velocity amplitude, and applied to the 14 TEPs then known. The importance of this is that whilst $g_b$ can be

7 This concept was also independently discovered by Beatty et al. (2007) and Winn et al. (2007a) – note that this does not necessarily require the eclipses to be total as claimed by Beatty et al. (2007).
found directly for a transiting planet, measuring its other physical properties (mass, radius, density) requires additional constraints such as are usually obtained from stellar theory, so are not empirical. Southworth et al. (2007b) found a significant correlation between $g_\text{b}$ and $P_{\text{orb}}$, although it is not yet clear whether this is a real effect or arises from selection biases. A plausible explanation is that short-period planets are close to their parent star and much of their atmosphere has been evaporated off by ultraviolet (UV) and X-ray irradiation. High-energy irradiation is believed to cause close-in extrasolar planets to lose their atmospheres (Lammer et al. 2003).

The $g_\text{b}$ values for the TEPs studied in this work have been determined from the light-curve analyses and published measurements of $K_\text{s}$ (Table 15). These have been augmented by literature values for the other known TEPs and are given in Table 16 and plotted in Fig. 21. The correlation is still clearly visible but is quite weak. The error bars for some of the planets could be decreased by performing light-curve analyses similar to those presented in this work. The fractional radii from the light-curve analyses are sensitive to the amount of stellar irradiation intercepted by the transiting planets, but plots of $r_\text{s}$ and $r_\text{b}$ show no correlation with $P_{\text{orb}}$.

### Table 15. Stellar velocity amplitudes for the systems studied here.

<table>
<thead>
<tr>
<th>System</th>
<th>$K_\text{s} , (\text{m s}^{-1})$</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>TrES-1</td>
<td>115.2 ± 6.2</td>
<td>Alonso et al. (2004)</td>
</tr>
<tr>
<td>TrES-2</td>
<td>181.3 ± 2.6</td>
<td>O’Donovan et al. (2006)</td>
</tr>
<tr>
<td>XO-1</td>
<td>116.0 ± 9.0</td>
<td>McCullough et al. (2006)</td>
</tr>
<tr>
<td>WASP-1</td>
<td>114 ± 13</td>
<td>Collier Cameron et al. (2007)</td>
</tr>
<tr>
<td>WASP-2</td>
<td>155 ± 7</td>
<td>Collier Cameron et al. (2007)</td>
</tr>
<tr>
<td>HAT-P-1</td>
<td>60.3 ± 2.1</td>
<td>Bakos et al. (2007a)</td>
</tr>
<tr>
<td>OGLE-TR-10</td>
<td>81 ± 17</td>
<td>Bouchy et al. (2005a)</td>
</tr>
<tr>
<td>OGLE-TR-10</td>
<td>80 ± 25</td>
<td>Konacki et al. (2005)</td>
</tr>
<tr>
<td>OGLE-TR-10</td>
<td>80.3 ± 14.1</td>
<td>(Adopted in this work)</td>
</tr>
<tr>
<td>OGLE-TR-56</td>
<td>212 ± 22</td>
<td>Bouchy et al. (2005a)</td>
</tr>
<tr>
<td>OGLE-TR-111</td>
<td>78 ± 14</td>
<td>Pont et al. (2004)</td>
</tr>
<tr>
<td>OGLE-TR-132</td>
<td>141 ± 42</td>
<td>Bouchy et al. (2004)</td>
</tr>
<tr>
<td>GJ 436</td>
<td>18.34 ± 0.52</td>
<td>Maness et al. (2007)</td>
</tr>
<tr>
<td>HD 149026</td>
<td>43.3 ± 1.2</td>
<td>Sato et al. (2005)</td>
</tr>
<tr>
<td>HD 189733</td>
<td>205 ± 6</td>
<td>Bouchy et al. (2005b)</td>
</tr>
<tr>
<td>HD 209458</td>
<td>85.1 ± 1.0</td>
<td>Naef et al. (2004)</td>
</tr>
</tbody>
</table>

### Table 16. Measured planetary surface gravities for the systems studied here (upper part of table) and for the other known TEPs (lower part of table). References are entirely parenthesized if the surface gravity has been calculated from the planetary properties ($M_\text{p}$ and $R_\text{p}$) given in that work.

<table>
<thead>
<tr>
<th>System</th>
<th>$g_\text{b} , (\text{m s}^{-1})$</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>TrES-1</td>
<td>15.6 ± 1.2</td>
<td>This work</td>
</tr>
<tr>
<td>TrES-2</td>
<td>19.9 ± 1.2</td>
<td>This work</td>
</tr>
<tr>
<td>XO-1</td>
<td>15.8 ± 1.5</td>
<td>This work</td>
</tr>
<tr>
<td>WASP-1</td>
<td>9.9 ± 1.7</td>
<td>This work</td>
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<tr>
<td>WASP-2</td>
<td>19.7 ± 2.4</td>
<td>This work</td>
</tr>
<tr>
<td>HAT-P-1</td>
<td>9.05 ± 0.66</td>
<td>This work</td>
</tr>
<tr>
<td>OGLE-TR-10</td>
<td>5.7 ± 1.2</td>
<td>This work</td>
</tr>
<tr>
<td>OGLE-TR-56</td>
<td>22.2 ± 6.6</td>
<td>This work</td>
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<tr>
<td>OGLE-TR-111</td>
<td>11.5 ± 2.5</td>
<td>This work</td>
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<tr>
<td>OGLE-TR-132</td>
<td>15.6 ± 6.1</td>
<td>This work</td>
</tr>
<tr>
<td>GJ 436</td>
<td>12.8 ± 1.2</td>
<td>This work</td>
</tr>
<tr>
<td>HD 149026</td>
<td>23.7 ± 1.2</td>
<td>This work</td>
</tr>
<tr>
<td>HD 189733</td>
<td>22.0 ± 1.4</td>
<td>This work</td>
</tr>
<tr>
<td>HD 209458</td>
<td>9.08 ± 0.17</td>
<td>This work</td>
</tr>
<tr>
<td>TrES-3</td>
<td>28.4 ± 4.2</td>
<td>O’Donovan et al. (2006)</td>
</tr>
<tr>
<td>TrES-4</td>
<td>7.43 ± 0.65</td>
<td>O’Donovan et al. (2007)</td>
</tr>
<tr>
<td>XO-2</td>
<td>14.9 ± 1.7</td>
<td>Burke et al. (2007)</td>
</tr>
<tr>
<td>XO-3</td>
<td>89 ± 11</td>
<td>Johns-Krull et al. (2007)</td>
</tr>
<tr>
<td>WASP-3</td>
<td>23.4 ± 5.9</td>
<td>Pollacco et al. (2007)</td>
</tr>
<tr>
<td>WASP-4</td>
<td>13.9 ± 1.3</td>
<td>Wilson et al. (2008)</td>
</tr>
<tr>
<td>WASP-5</td>
<td>30.5 ± 2.4</td>
<td>Anderson et al. (2008)</td>
</tr>
<tr>
<td>OGLE-TR-113</td>
<td>27.6 ± 4.1</td>
<td>Gillon et al. (2006)</td>
</tr>
<tr>
<td>OGLE-TR-182</td>
<td>19.8 ± 2.5</td>
<td>Pont et al. (2007c)</td>
</tr>
<tr>
<td>OGLE-TR-211</td>
<td>13.7 ± 3.0</td>
<td>Udalski et al. (2007)</td>
</tr>
<tr>
<td>HAT-P-2</td>
<td>236.1 ± 4.2</td>
<td>Loeillet et al. (2007)</td>
</tr>
<tr>
<td>HAT-P-3</td>
<td>20.4 ± 3.1</td>
<td>Torres (2007)</td>
</tr>
<tr>
<td>HAT-P-4</td>
<td>10.47 ± 0.48</td>
<td>Kovács et al. (2007)</td>
</tr>
<tr>
<td>HAT-P-5</td>
<td>16.5 ± 1.9</td>
<td>Bakos et al. (2007b)</td>
</tr>
<tr>
<td>HAT-P-6</td>
<td>14.8 ± 1.0</td>
<td>Noyes et al. (2008)</td>
</tr>
<tr>
<td>HD 17156</td>
<td>11.6 ± 5.7</td>
<td>Barbieri et al. (2007)</td>
</tr>
</tbody>
</table>

### 5 SUMMARY AND CONCLUSIONS

At this time over 30 TEPs are known, but their properties have been obtained using a variety of different methods. I have presented detailed light-curve analyses of 14 TEPs for which good light curves...
are available, paying particular attention to the importance of LD and the assessment of random and systematic errors. In a second paper the results of these analyses will be used to determine the physical properties of each system, in a homogeneous way, using the predictions of theoretical stellar models and concentrating on obtaining the most reliable values and uncertainties.

The parameters found in my light-curve analyses are generally in good agreement with published studies. However, the uncertainties found in this study are often significantly larger (by factors of up to 3). This stems from including several sources of error (Monte Carlo simulations for random errors, a residual permutation algorithm to assess systematic errors and the effect of using different LD laws), some of which are not incorporated into previous works. Although my uncertainty estimates are generally larger than those from other studies, solutions of different light curves for individual systems still do not agree to within these errors. This problem is clear for the two well-studied systems HD 189733 and HD 209458, both of which have three different high-quality light curves available. The worst discrepancy occurs for the ratio of the radii (6.7σ for HD 189733 and 3.7σ for HD 209458), which is primarily dependent on the observed transit depth. This indicates that systematic errors remain in the light curves which cannot be detected through analysis of only one data set; definitive results for an individual TEP can only be obtained when at least three independent light curves are obtained and analysed.

I was not able to reproduce published solutions of the light curves for HD 149026, which contain a high-density planet. The three light curves of this system give quite different results and it is clear that further observations are needed. My solution has a higher orbital inclination (corresponding to a central transit) and leads to smaller radii for both the star and planet, which suggests that HD 149026 b is even more dense than currently thought.

An improved light curve is also needed for OGLE-TR-132 because the current best data set does not cover the full transit. Further observations would also be useful for TrES-2, the only system where light-curve solutions with one or two fitted LDCs do not agree well. Additional investigations of OGLE-TR-10 would also be useful, because published studies of this object give widely varying results. The correlation between orbital period and planetary surface gravity (first noticed by Southworth et al. 2007b) remains visible when the new TEPs are included, although there are a few outliers with much higher gravities. Several of the surface gravity measurements are quite imprecise, with the main contribution to their uncertainty arising from the stellar velocity amplitude rather than the light-curve analyses. New spectroscopic radial velocity studies for XO-1, WASP-1, WASP-2 and the OGLE transiting planets are needed to improve our understanding of the physical properties of these systems.

5.1 Treatment of limb darkening

One potentially thorny problem in the study of the light curves of TEPs is how much effect the use of different LD laws has on the light-curve solutions. The linear LD law is clearly inadequate when studying the high-quality HST light curves of HD 209458 and can be ruled out at the 99.99 per cent level. This is in agreement with results from the study of eclipsing binary stars (Southworth et al. 2007a) and with the predictions of stellar model atmospheres (Van Hamme 1993; Claret 2000). However, the linear law is adequate for most of the data sets studied in this work (particularly those from longer wavelengths).

Solutions were also done using the two-coefficient quadratic, square root, logarithmic and cubic LD laws. It is usually not possible to measure both LDCs for one star because they are strongly correlated, but this means that one LDC can be fixed at a reasonable value without making a significant difference to the light-curve solution. When both LDCs are included as fitted parameters, the cubic law gives the best-determined LDCs and the square-root law suffers...
from the biggest correlations. The quadratic and cubic laws generally perform well, but the usefulness of the cubic law is restricted as there are no theoretical predictions available. In general, though, there is little to choose between solutions using the four different LD laws: the solutions of all but the highest quality transit light curves are not adversely affected by the choice of LD law. This is good news for studies of transiting planets (but bad news for studies of stellar LD).

Additional solutions with all LDCs fixed were calculated for TrES-1, TrES-2 and XO-1. In general these give results in (mostly) acceptable agreement with other solutions, but with substantially smaller error bars. It is therefore clear that fixing coefficients at theoretical values not only allows biases to creep in to the results, but also makes the uncertainties too optimistic.

Despite the previous point, a comparison between measured LDCs and those predicted using stellar model atmospheres is a promising way of improving our knowledge of stellar atmospheres. It is known that current stellar model atmospheres do not reproduce the LD of stars very well (A. Claret, private communication). Whilst a detailed study is beyond the scope of the present work, a limited comparison was carried out between the LDCs measured from light curves of HD 209458 in 10 passbands spread through the optical wavelength range. Predicted LDCs were unable to match the measured coefficients for either the linear or quadratic laws. A similar study by Tingley, Thurl & Sackett (2006) also found a disagreement between the observed and predicted colour dependence of limb-darkened transit light curves.

5.2 Looking ahead

Much of our understanding of extrasolar planets rests on the transiting systems, and this work confirms that these can be studied to high accuracy. New light curves of HD 149026, TrES-2, OGLE-TR-10, OGLE-TR-56, OGLE-TR-132 and GI 436 would help to improve our understanding further, as would additional radial velocity studies of XO-1, WASP-1, WASP-2 and the OGLE transiting planets. In Paper II (in preparation) the light-curve analysis results from the current paper will be used to determine homogeneous sets of physical properties for the 14 TEPs studied here, with the aim of improving the prospects for statistical studies of these and other systems.

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SUPPLEMENTARY MATERIAL

The following supplementary material is available for this article.

Appendix A. Results of the light-curve analyses.

This material is available as part of the online paper from: http://www.blackwell-synergy.com/doi/abs/10.1111/j.1365-2966.2008.13145.x (this link will take you to the article abstract).

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